

QUESTION BANK

1. Which of the following signals is/ are periodic?
 - (a) $x(t) = \cos 2t + \cos 3t + \cos 5t$
 - (b) $x(t) = \exp(j8\pi t)$
 - (c) $x(t) = \exp(-7t) \sin 10\pi t$
 - (d) $x(t) = \cos 2t \cos 4t$

2. **Assertion (A)** : An LTI discrete system represented by the difference equations $y(n + 2) - 5y(n + 1) + 6y(n) = x(n)$ is unstable
Reason (R): A system is unstable if the roots of the characteristic equation lie outside the unit circle.
 - (a) Both A and R are true and R is the correct explanation of A
 - (b) Both A and R are true but R is NOT the correct explanation of A
 - (c) A is true but R is false
 - (d) A is false but R is true

3. Consider a random sinusoidal signal $x(t) = \sin(\omega_0 t + \phi)$ where a random variable ' ϕ ' is uniformly distributed in the range $+\pi/2$. The mean value of $x(t)$ is
 - (a) zero
 - (b) $\frac{2}{\pi} \sin(\omega_0 t)$
 - (c) $\frac{2}{\pi} \cos(\omega_0 t)$
 - (d) $\frac{2}{\pi}$

4. The function $\delta(2n)$ is equal to
 - (a) $\delta(n)$
 - (b) $\frac{1}{2} \delta(n)$
 - (c) $2\delta(n)$
 - (d) $2\delta\left(\frac{n}{2}\right)$

5. Let $\delta(t)$ denote the delta function. The value of the integral $\int_{-\infty}^{\infty} \delta(t) \cos\left(\frac{3t}{2}\right) dt$ is
 - (a) 1
 - (b) -1
 - (c) 0
 - (d) $\frac{\pi}{2}$

6. If a signal $f(t)$ has energy E, the energy of the signal $f(2t)$ is equal to
 - (a) E
 - (b) $E/2$
 - (c) $2E$
 - (d) $4E$

7. If a function $f(t)u(t)$ is shifted to right side by t_0 , then the function can be expressed as
 - (a) $f(t-t_0)u(t)$
 - (b) $f(t)u(t-t_0)$
 - (c) $f(t-t_0)u(t-t_0)$
 - (d) $f(t+t_0)u(t-t_0)$

8. The color T.V. picture signal is a
 - (a) Single-channel, one-dimensional signal
 - (b) single-channel, three dimensional signal
 - (c) three-channel, one-dimensional signal
 - (d) three-channel, three-dimensional signal

9. Consider the signals $x_1(t) = 2\sin \pi t + \cos 4\pi t$ and $x_2(t) = 2\sin 5\pi t + 3\sin 13\pi t$
 - (a) Both the signals are periodic
 - (b) Both the signals are not periodic
 - (c) x_1 is periodic, but x_2 is not periodic
 - (d) x_1 is not periodic, but x_2 is periodic

10. The sum of two or more arbitrary sinusoids is
 - (a) always periodic
 - (b) Periodic under certain conditions
 - (c) Never periodic
 - (d) Periodic only if all the sinusoids are identical in frequency and phase

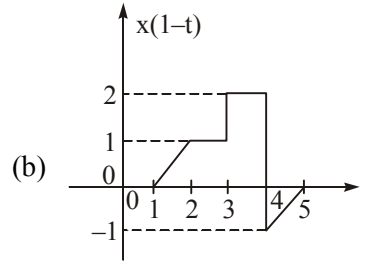
11. Which one of the following must be satisfied if a signal is to be periodic for $-\infty < t < \infty$?
 - (a) $x(t + T_0) = x(t)$
 - (b) $x(t + T_0) = dx(t) / dt$
 - (c) $x(t + T_0) = \int_t^{T_0} x(t) dt$
 - (d) $x(t + T_0) = x(t) + kT_0$

21. Consider two signals $x_1(t) = e^{j20t}$ and $x_2(t) = e^{(-2+j)t}$. Which one of the following statements is correct?
- Both $x_1(t)$ and $x_2(t)$ are periodic
 - $x_1(t)$ is periodic but $x_2(t)$ is not periodic
 - $x_2(t)$ is periodic but $x_1(t)$ is not periodic
 - Neither $x_1(t)$ nor $x_2(t)$ is periodic
22. If v-i characteristic of a circuit is given by $v(t) = ti(t) + 2$, the circuit is of which type?
- Linear and time invariant
 - Linear and time variant
 - Non-linear and time invariants
 - Non-linear and time variant
23. Which one of the following function is a periodic one?
- $\sin(10\pi t) + \sin(20\pi t)$
 - $\sin(10t) + \sin(20\pi t)$
 - $\sin(10\pi t) + \sin(20t)$
 - $\sin(10t) + \sin(25t)$
24. A signal $x_1(t)$ and $x_2(t)$ constitute the real and imaginary parts respectively of a complex valued signal $x(t)$. What form of waveform does $x(t)$ possess?
- Real symmetric
 - Complex symmetric
 - Asymmetric
 - Conjugate symmetric
25. If a random process $X(t)$ is periodic then, statistical averages
- and time averages are different
 - and time averages are same
 - are greater than time averages
 - are smaller than time averages
26. The system represented by the input-output relationship $y(t) = \int_{-\infty}^{5t} x(\tau) d\tau, t > 0$ is
- Linear and causal
 - Linear but not causal
 - Causal but not linear
 - Neither linear nor causal
27. The period of the signal $x(t) = 8 \sin\left(0.8\pi t + \frac{\pi}{4}\right)$ is
- 0.4 π s
 - 0.8 π s
 - 1.25 s
 - 2.5 s
28. A signal $f(t)$ is described as
- $$f(t) = \begin{cases} [t - |t|] & \text{when } |t| \leq 1 \\ 0 & \text{when } |t| > 1 \end{cases}$$
- This represents the unit.
- sinc function
 - area triangular function
 - signum function
 - parabolic function
29. Match List-I with List-II and select the correct answer using the code given below the lists:
- | List-I | List-II |
|--------------------|---|
| A. Even signal | 1. $x(n) = \left(\frac{1}{4}\right)^n u(n)$ |
| B. Causal signal | 2. $x(-n) = x(n)$ |
| C. Periodic signal | 3. $x(t)u(t)$ |
| D. Energy signal | 4. $x(n) = x(n + N)$ |
- Codes:**
- | | A | B | C | D |
|-----|---|---|---|---|
| (a) | 2 | 3 | 4 | 1 |
| (b) | 1 | 3 | 4 | 2 |
| (c) | 2 | 4 | 3 | 1 |
| (d) | 1 | 4 | 3 | 2 |

30. The period of the signal

$$x(t) = 10\sin 12\pi t + 4\cos 18\pi t$$

- (a) $\frac{\pi}{4}$ (b) $\frac{1}{6}$
 (c) $\frac{1}{9}$ (d) $\frac{1}{3}$

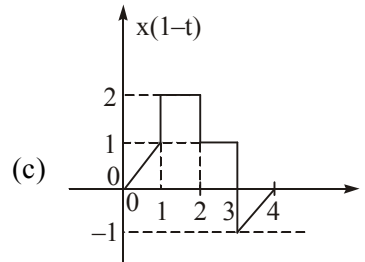


31. If, (i) $x_1(t) = 2\sin\pi t + \cos 4\pi t$

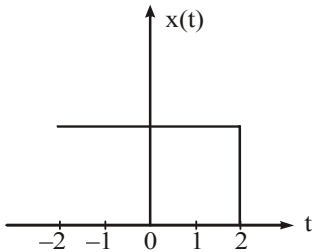
(ii) $x_2(t) = \sin 5\pi t + 3\sin 13\pi t$

Which of the above are periodic ?

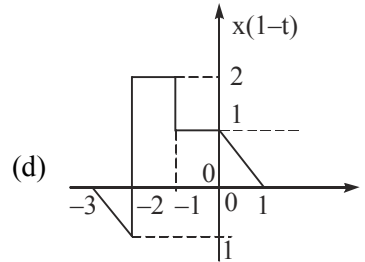
- (a) (i) only (b) (ii) only
 (c) both (i) and (ii) (d) none of the above



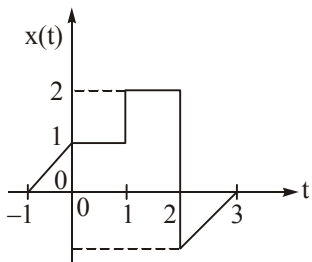
32. The mathematical model of the below shown signal is



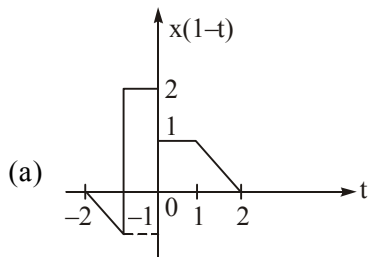
- (a) $x(t) = u(2+t)$
 (b) $x(t) = u(t-2)$
 (c) $x(t) = u(2-t)$
 (d) $x(t) = u(t-1)$



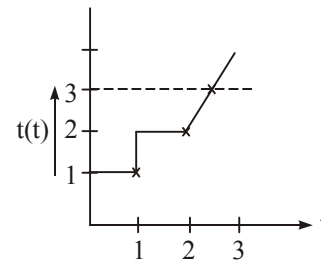
33. If a plot of signal $x(t)$ is as shown in the figure-1.



then the plot of the signal $x(1-t)$ will be



34. Consider the following waveform diagram



Which one of the following gives the correct description of the waveform shown in the above diagram?

- (a) $u(t) + u(t-1)$
 (b) $u(t) + u(t-1)u(t-1)$
 (c) $u(t) + u(t-1)u(t-2)u(t-2)$
 (d) $u(t) + (t-2)u(t-2)$

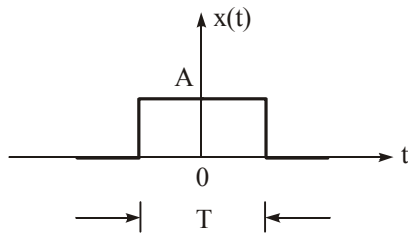
35. $x[n]$ is defined as

$$x[n] = \begin{cases} 0 & \text{for } n < -2 \text{ or } n > 4 \\ 1, & \text{otherwise} \end{cases}$$

Determine the value of n for which $x[-n-2]$ is guaranteed to be zero.

- (a) $n < 1$ and $n > 7$
- (b) $n < -4$ and $n > 2$
- (c) $n < -6$ and $n > 0$
- (d) $n < -2$ and $n > 4$

36. What is the total energy of the rectangular pulse shown in the figure given above?



- (a) AT
- (b) A^2T
- (c) A^2T^2
- (d) AT^2

Linked Answer Question 37 & 38

The impulse response $h(t)$ of a linear time-invariant continuous time system is given by $h(t) = \exp(-2t)u(t)$, where $u(t)$ denotes the unit step function.

37. What is the period of the sinusoidal signal $x(n) = 5 \cos [0.2\pi n]$?

- (a) 10
- (b) 5
- (c) 1
- (d) 0

38. If $x(t)$ is a periodic signal with Fourier series coefficient C_n and $y(t) = x(at)$. The average powers in $x(t)$ and $y(t)$ are P_x & P_y respectively, then

- (a) $P_y = aP_x$
- (b) $P_y = a^2P(x)$
- (c) $P_y = P(x)/a^2$
- (d) $P_y = P_x$

39. **Statement 1:** $x[n] = \cos\left[\frac{1}{4}n\right]$ is non periodic.

Statement 2: $x(t) = e^{i\left[\left(\frac{\pi}{2}\right)t-1\right]}$ is periodic.

Choose correct option

- (a) Both statement are true
- (b) Statement 1 is false, but statement 2 is true
- (c) Statement 1 is true, but statement 2 is false
- (d) Both statement are false

40. The discrete time signal $x(n)$ is defined by

$$x(n) = \begin{cases} 1 & n = 1 \\ -1 & n = -1 \\ 0 & n = 0 \text{ and } |n| > 1 \end{cases}$$

Which one of the following is the composite signal $y(n) = x(n) + x(-n)$ for all integer values of n ?

- (a) 0
- (b) 2
- (c) ∞
- (d) $-\infty$

41. Match List-I (Characteristic of $f(t)$) with List-II (Functions) and select the correct answer using the codes given below the lists :

List-I

- A. $f(t)(1-u(t)) = 0$
- B. $\frac{f(t) + Kdf(t)}{dt} = 0$; K is a positive constant
- C. $f(t) + K \frac{d^2f(t)}{dt^2} = 0$; K is a positive constant
- D. $f(t)(g(t) - g(0)) = 0$; for any arbitrary $g(t)$

List-II

- 1. Decaying exponential
- 2. Growing exponential
- 3. Impulse
- 4. Causal
- 5. Sinusoid

Codes: A B C D

- | | | | |
|-------|---|---|---|
| (a) 4 | 1 | 5 | 3 |
| (b) 1 | 4 | 5 | 3 |
| (c) 4 | 2 | 5 | 1 |
| (d) 2 | 5 | 4 | 1 |

42. Which one of the following is the mathematical representation for the average power of the signal $x(t)$?

- | | |
|---|---|
| (a) $\frac{1}{T} \int_0^T x(t) dt$ | (b) $\frac{1}{T} \int_0^T x^2(t) dt$ |
| (c) $\frac{1}{T} \int_{-T/2}^{T/2} x(t) dt$ | (d) $\lim_{T \rightarrow \infty} \frac{1}{T} \int_{-T/2}^{T/2} x^2(t) dt$ |

43. Consider the continuous time single $x(t) = \delta(t+2) - \delta(t-2)$. The value of E_∞ for

the signal $y(t) = \int_{-\infty}^1 x(\tau) d\tau$ is-

- | | |
|-------|-------|
| (a) 2 | (b) 0 |
| (c) 4 | (d) 1 |

44. The fundamental period of the signal

$$x[n] = 1 + e^{j4\pi n/7} - e^{j2\pi n/5}$$

- | | |
|---------|--------|
| (a) 35 | (b) 70 |
| (c) 140 | (d) 25 |

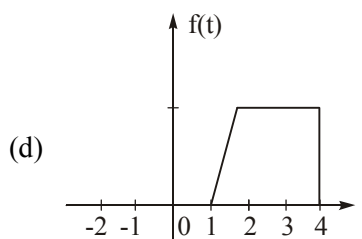
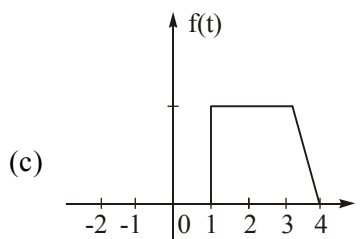
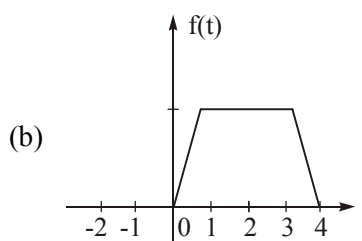
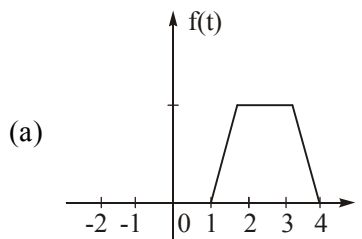
45. Which one of the following is correct? Energy of a power signal is

- | | |
|--------------|---------------------|
| (a) finite | (b) zero |
| (c) infinite | (d) between 1 and 2 |

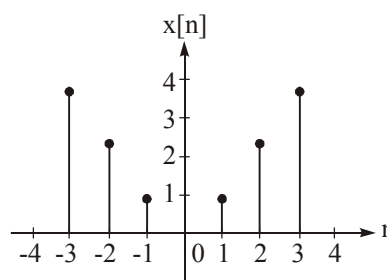
46. Given sinusoidal signal $x(t) = \cos(21t)$, with sampling interval T_s such that $x[n] = x(nT_s)$ is a periodic sequence. The fundamental period is, it, $T_s = 0.3\pi$ sec

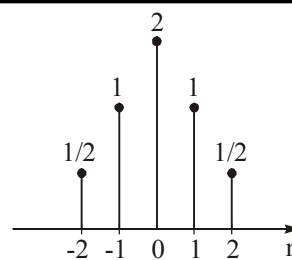
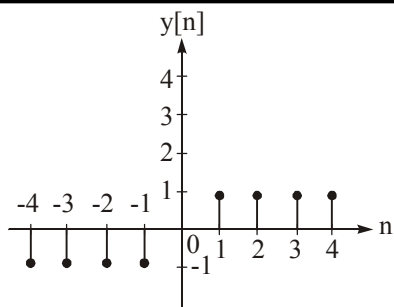
- | | |
|--------|--------|
| (a) 5 | (b) 10 |
| (c) 15 | (d) 20 |

47. The signal $f(t) = (t-1)u(t-1) - (t-2)u(t-2) - u(t-4)$ shows figure below

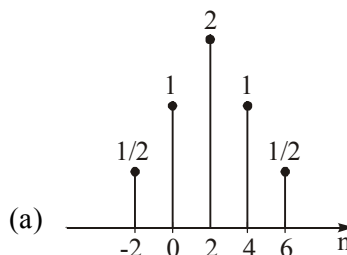
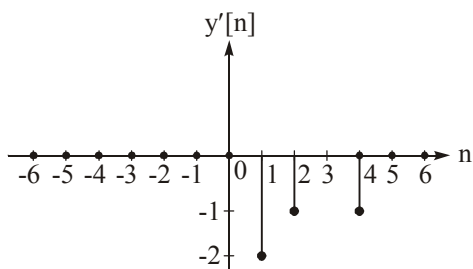


48. $x[n]$ and $y[n]$ are given below figure





the signal



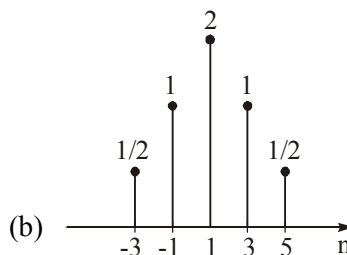
represents.

(a) $y'[n] = x[n-3] \cdot y[-n]$

(b) $y'[n] = x[3-n] \cdot y[-n]$

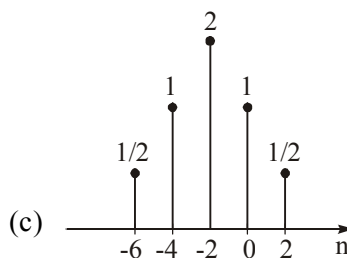
(c) $y'[n] = x[-n-3] \cdot y[-n]$

(d) $y'[n] = x[3-n] \cdot y[-n]$



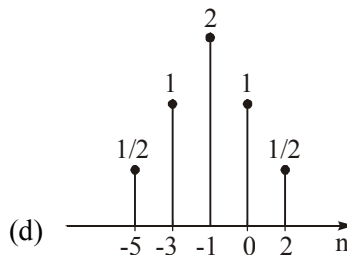
49. The signal $x(t) = A \cos(\omega t + \phi)$ is

- (a) an energy signal
- (b) a power signal
- (c) an energy as well as a power signal
- (d) neither an energy nor a power signal



50. A sequence $x(n)$ has non-zero values as shown in figure. The sequence

$$y(n) = \begin{cases} x\left(\frac{n}{2}-1\right) & \text{for 'n' even} \\ =0, & \text{for 'n' odd} \end{cases}$$



ANSWERS AND EXPLANATIONS

1. Ans. (a), (b), (c)

(i) $x(t) = \cos 2t + \cos 3t + \cos 5t$

$x(t) = x_1(t) + x_2(t) + x_3(t)$

Where, $x_1(t) = \cos 2t = \cos \omega_1 t$

$\Rightarrow \omega_1 = 2 = \frac{2\pi}{T_1}$ and $T_1 = \pi$

and $x_2(t) = \cos 3t = \cos \omega_2 t$

$\Rightarrow \omega_2 = 3 = \frac{2\pi}{T_2}$ and $T_2 = \frac{2\pi}{3}$

and $x_3(t) = \cos 5t = \cos \omega_3 t$

$\Rightarrow \omega_3 = 5 = \frac{2\pi}{T_3}$ and $T_3 = \frac{2\pi}{5}$

Ratio of time periods,

$\frac{T_1}{T_2} = \frac{\pi}{2\pi/3} = \frac{3}{2} = 1.5 = \text{Rational number}$

$\frac{T_1}{T_3} = \frac{\pi}{2\pi/5} = \frac{5}{2} = 2.5 = \text{Rational number}$

$\frac{T_2}{T_3} = \frac{2\pi/3}{2\pi/5} = \frac{5}{3} = 1.666 = \text{Rational number}$

Since ratios of time periods of signals are rational numbers so given signal is periodic.

Fundamental period,

$T_0 = \frac{\text{L.C.M. of numerator of } T_1, T_2 \text{ \& } T_3}{\text{H.C.F. of denominator of } T_1, T_2 \text{ \& } T_3}$

$\Rightarrow T_0 = \frac{\text{L.C.M. of } (2\pi, 2\pi, 2\pi)}{\text{H.C.F. of } (1, 3, 5)} = \frac{2\pi}{1} = 2\pi$

(ii) $x(t) = e^{j8\pi t} = e^{j\omega_0 t}$

where, $\omega_0 = \frac{2\pi}{T_0} = 8\pi$

$\Rightarrow T_0 = \frac{1}{4}$

So, signal is periodic.

(iii) $x(t) = e^{-7t} \sin 10\pi t$

Exponential decaying signals are non-periodic signals.

(iv) $x(t) = \cos 2t \cos 4t$

$= \frac{1}{2} \left[\cos \left(\frac{2+4}{2} t \right) + \cos \left(\frac{4-2}{2} t \right) \right]$

$= \frac{1}{2} [\cos 3t + \cos t] = \frac{1}{2} \cos 3t + \frac{1}{2} \cos t = x_1(t) + x_2(t)$

where, $x_1(t) = \frac{1}{2} \cos 3t = \frac{1}{2} \cos \omega_1 t$

$\Rightarrow \omega_1 = \frac{2\pi}{T_1} = 3$ & $T_1 = \frac{2\pi}{3}$

and $x_2(t) = \frac{1}{2} \cos t = \frac{1}{2} \cos \omega_2 t$

$\Rightarrow \omega_2 = \frac{2\pi}{T_2} = 1$ & $T_2 = 2\pi$

Ratio of time periods,

$\frac{T_1}{T_2} = \frac{2\pi/3}{2\pi} = \frac{1}{3} = \text{Rational number}$

Since ratio of time periods is rational number so signal is periodic. Fundamental period of $x(t)$,

$T_0 = \frac{\text{L.C.M. of } (2\pi, 2\pi)}{\text{H.C.F. of } (1, 3)} = \frac{2\pi}{1} = 2\pi$

2. Ans. (a)

3. Ans. (b)

4. Ans. (b)

5. Ans. (a)

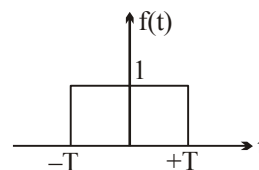
According to sampling property of impulse function,,

$\int_{-\infty}^{\infty} x(t) \delta(t - t_0) dt = x(t_0)$

if $x(t) = \cos \frac{3}{2} t$ and $t_0 = 0$

then, $\int_{-\infty}^{\infty} \cos \left(\frac{3}{2} t \right) \delta(t) dt = \cos \frac{3}{2} (0) = 1$

6. Ans. (b)



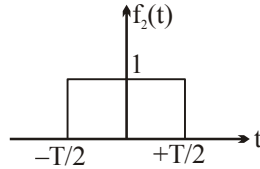
Let $f(t) = 1$; $-T < t < T$
 $= 0$ ' $|t| > T$

Energy carried by $f(t)$,

$$E_{\infty} = \int_{-\infty}^{\infty} [f(t)]^2 dt,$$

$$E_{\infty} = \int_{-T}^{+T} [1]^2 dt = 2T$$

Let $f_2(t) = f(2t)$



$$\Rightarrow f_2(t) = 1 \quad ; \quad -T/2 < t < T/2$$

$$\therefore E_2 = \int_{-\infty}^{\infty} [f_2(t)]^2 dt = \int_{-\infty}^{\infty} [f(2t)]^2 dt = \int_{-T/2}^{+T/2} (1)^2 dt = T$$

$$\Rightarrow E_2 = \frac{E}{2}$$

7. *Ans. (c)*

8. *Ans. (b)*

9. *Ans. (c)*

10. *Ans. (b)*

11. *Ans. (a)*

12. *Ans. (d)*

13. *Ans. (a)*

Given, $x[n] = [-4 - j5 \quad 1 + j2 \quad 4]$

$$\Rightarrow x^*[-n] = [4 \quad 1 - j2 \quad -4 + j5]$$

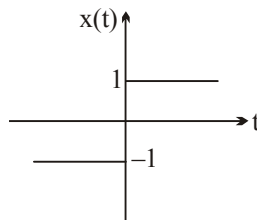
Conjugate antisymmetric part of $x[n]$ is given by,

$$x_{CAS} = \frac{x[n] - x^*[-n]}{2}$$

$$x_{CAS} = \left[\frac{-4 - j5 - 4}{2} \quad \frac{1 + j2 - 1 + 2j}{2} \quad \frac{4 + 4 - j5}{2} \right]$$

$$= [-4 - j2.5 \quad j2 \quad 4 - j2.5]$$

14. *Ans. (a)*



$$x(t) = u(t)$$

$$t > 0$$

$$= -u(-t)$$

$$t < 0$$

$$\therefore x(t) = u(t) - u(-t)$$

Even part of a signal $f(t)$ is given by,

$$f_e(t) = \frac{1}{2}[f(t) + f(-t)]$$

for step function, $f(t) = u(t)$,

$$u_e(t) = \frac{1}{2}[u(t) + u(-t)] = \frac{1}{2}$$

Odd part of a signal $f(t)$ is given by,

$$f_o(t) = \frac{1}{2}[f(t) - f(-t)]$$

for $f(t) = u(t)$

$$\Rightarrow u_o(t) = \frac{1}{2}[u(t) - u(-t)] = \frac{1}{2}x(t)$$

15. *Ans. (d)*

16. *Ans. (a)*

17. *Ans. (d)*

18. *Ans. (d)*

19. *Ans. (d)*

Dirac delta function is defined by,

$$\delta(t) = 0 \quad ; \quad t \neq 0$$

$$\text{and} \quad \int_{-\infty}^{\infty} \delta(t) dt = 1$$

20. *Ans. (d)*

A bounded signal is always finite.

21. *Ans. (b)*

22. *Ans. (d)*

23. *Ans. (a,d)*

24. *Ans. (d)*

25. *Ans. (b)*

26. *Ans. (b)*

(i) A system is causal if its present output depends on present and/or past values of inputs. But time scaling gives non causal system.

(ii) A system is time invariant system if time shift in input gives identical shift in output. But time scaling results in a time varying system.

(iii) A system is unstable if bounded input gives unbounded output. So integrator is an example of unstable system.

(iv) The system is linear if a time shift input leads to identical shift in output.

Given, $y(t) = \int_{-\infty}^{5t} x(\tau) d\tau, t > 0$

Conclusion :

A. Given system is a non-causal system as it has time scaling.

B. The given system is linear because it is an integrator which is an example of linear system.

C. The system is time varying because of time scaling.

D. The system output is unbounded for bounded value of $x(t)$. So it is an example of unstable system.

27. Ans. (d)

Given, $x(t) = 8 \sin\left(0.8\pi t + \frac{\pi}{4}\right)$

$\Rightarrow x(t) = 8 \sin\left(\omega_0 t + \frac{\pi}{4}\right)$

where, $\omega_0 = 0.8\pi = \frac{2\pi}{T_0}$ = fundamental frequency

of the signal.

and T_0 is fundamental period of $x(t)$

$\Rightarrow T_0 = \frac{2\pi}{0.8\pi} = 2.5 \text{sec}$

Note : A continuous time sinusoidal signal having single sine or cosine term is always periodic in nature.

28. Ans. (b)

29. Ans. (a)

30. Ans. (d)

31. Ans. (c)

32. Ans. (c)

33. Ans. (a)

34. Ans. (c)

35. Ans. (c)

36. Ans. (b)

37. Ans. (a)

38. Ans. (d)

39. Ans. (a)

40. Ans. (a)

41. Ans. (a)

42. Ans. (d)

43. Ans. (c)

44. Ans. (a)

45. Ans. (c)

46. Ans. (d)

$$T_0 = \frac{2\pi}{\omega_0} = \frac{2\pi}{21}$$

and $\frac{T_s}{T_0} = \frac{T_3}{(2\pi/21)} = \frac{m}{N_0}$

$$\Rightarrow T_s = \frac{m}{N_0} \cdot \frac{2\pi}{21}$$

$$\Rightarrow 0.3\pi = \frac{m}{N_0} \cdot \frac{2\pi}{21}$$

$$\Rightarrow N_0 = \frac{20}{63} m$$

for minimum, $m = 63$, then $N_0 = 20$ (fundamental period)

47. Ans. (d)

48. Ans. (d)

49. Ans. (b)

50. Ans. (a)

$$y(n) = x\left(\frac{n}{2} - 1\right), n \text{ is even}$$

= 0 ; for, 'n' is odd.

$$n = 0, y(n) = x(-1) = 1$$

$$n = 2, y(n) = x(0) = 2$$

$$n = 4, y(n) = x(1) = 1$$

$$n = 6, y(n) = x(2) = 1/2$$

